

PEA Association Pvt. Ltd. Thapathali, Kathmandu, Tel: 5345730, 5357187
2080-2-20 Hints & Solution

Section - I

1. (b) $\vec{A} \cdot \vec{B} = 0$

or, $(\cos\omega t\hat{i} + \sin\omega t\hat{j}) \cdot (\cos\frac{\omega t}{2}\hat{i} + \sin\frac{\omega t}{2}\hat{j}) = 0$

or, $\cos\omega t \cos\frac{\omega t}{2} + \sin\omega t \sin\frac{\omega t}{2} = 0$

or, $\cos\left(\omega t - \frac{\omega t}{2}\right) = 0 = \cos\frac{\pi}{2}$

or, $\omega t - \frac{\omega t}{2} = \frac{\pi}{2}$ or, $\frac{\omega t}{2} = \frac{\pi}{2}$ or, $t = \frac{\pi}{\omega}$

2. (b) If a body have constant velocity then its speed must be constant.

3. (d) $R - mg = ma$

or, $R = m(g + a)$

4. (c) Moment of inertia first decreases

So the angular speed increases again the moment of inertia increases so the angular speed decreases.

5. (b) Metal of higher linear expansivity lies on convex side.

6. (a) Black body is good absorber as well as good radiator.

7. (a) $n = \frac{V}{4l}$

if length is double then

$$n' = \frac{V}{4l'} = \frac{V}{4 \times 2l} = \frac{n}{2}$$

8. (d) $I_{\max} = I + I + 2\sqrt{II} \cos 0^\circ$
 $= 4I$

9. (a) $F = EQ = \frac{\sigma}{2\epsilon_0} = \frac{Q^2}{2\epsilon_0 A} = \frac{(CV)^2}{2C.d} = \frac{1}{2} \frac{CV^2}{d}$

10. (d) When charge θ is brought close to metal cube then equal and opposite charge is induced near to charge and equal and same charge is induced away from it keep.
 Total charge zero inside cube.

11. (c) $\frac{R'}{R} = \left(\frac{2l}{l}\right)^2 = 4$

∴ $R' = 4R$

12. (d) $I_1^2 R_1 t = I_2^2 R_2 t$

or, $\left(\frac{E}{R_1 + r}\right)^2 R_1 = \left(\frac{E}{R_2 + r}\right)^2 R_2$

or, $\left(\frac{R_2 + r}{R_1 + r}\right)^2 = \frac{R_2}{R_1}$

or, $\frac{R_2 + r}{R_1 + r} = \sqrt{\frac{R_2}{R_1}}$

or, $R_2\sqrt{R_1} + r\sqrt{R_1} = R_1\sqrt{R_2}\sqrt{R_2} + r\sqrt{R_2}$

or, $R_2\sqrt{R_1} - R_1\sqrt{R_2} = r\sqrt{R_2} - r\sqrt{R_1}$

or, $\sqrt{R_1}\sqrt{R_2}(\sqrt{R_2} - \sqrt{R_1}) = r\sqrt{R_2} - r\sqrt{R_1}$

or, $r = \sqrt{R_1}\sqrt{R_2}$

13. (c) $I_{\max} = \sqrt{\left(\frac{I_1}{\sqrt{2}}\right)^2 + \left(\frac{I_2}{\sqrt{2}}\right)^2} = \sqrt{\frac{I_1^2 + I_2^2}{2}}$

14. (c) Convex mirror form virtual image for real object

15. (c)

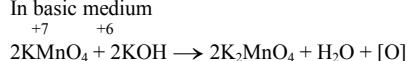
16. (d) $\frac{\left(\frac{e}{m}\right)_p}{\left(\frac{2e}{4m}\right)_a} = \frac{e}{m} \times \frac{4m}{2e} = 2:1$

17. (d) $\beta = 60^\circ$

Voltage gain = $\frac{V_{\text{out}}}{V_{\text{in}}} = \frac{I_b R_{\text{out}}}{I_b R_{\text{in}}} = \beta \times \frac{5000}{500} = 600$

18. (c)

19. (a) In basic medium



EW of KMnO₄ = $\frac{158}{1} = 158$

$\frac{W}{E} = \frac{N \times V_{\text{ml}}}{1000}$

$x = \frac{0.1 \times 100}{1000}$

$x = \frac{0.1 \times 100 \times 158}{1000} = 1.58$

21. (b)

$1.8L = 1.8 \times 1000 = 1800 \text{ ml}$

Mass = $V \times D = 1800 \times 1 = 1800 \text{ g}$

18g water = 1 mole

$1800 \text{ g water} = \frac{1}{18} \times 1800 = 100 \text{ moles}$

22. (a)

23. (a) (a) 24 mg

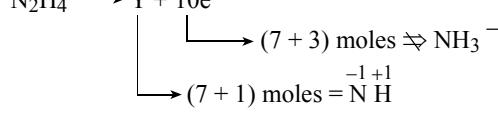
(b) 1 mole = 30g

0.9 moles = $30 \times 0.9 = 27 \text{ g}$

(c) 22.4L N₂ = 28g

(d) $6.023 \times 10^{23} \text{ O}_2 \text{ molecules} = 32 \text{ g}$

24. (a)



25. (b)

26. (d)

27. (c)

28. (b)

29. (c) No. of non-empty proper subsets = $2^n - 2$
 $= 2^4 - 2 = 14$

30. (c) $|3 - x| < 4$

$\Rightarrow -4 < 3 - x < 4$

$\Rightarrow -7 < -x < 1$

$\Rightarrow -1 < x < 7$

31. (a) $\frac{b - c \cos A}{a - c \cos B} = \frac{a \cos C + c \cos A - c \cos A}{b \cos C + c \cos B - c \cos B} = \frac{a}{b}$

32. (b) $\sin^{-1} \left(-\frac{\sqrt{3}}{2} \right) = \sin^{-1} \left[\sin \left(-\frac{\pi}{3} \right) \right] = -\frac{\pi}{3}$

33. (d) Here, n = 10, r = 2

Total no. of hand shakes = ${}^n C_r = {}^{10} C_2 = 45$

34. (a) The system has no solution if D = 0

i.e. $\begin{vmatrix} k & 3 \\ 1 & 2 \end{vmatrix} = 0$

$\Rightarrow 2k - 3 = 0 \Rightarrow k = \frac{3}{2}$

35. (b) $\log_e(1 - 2x)$ is valid if $-1 \leq 2x < 1$

$\Rightarrow -\frac{1}{2} \leq x < \frac{1}{2}$

36. (b) We have, $(1 + x)^n = {}^n C_0 + {}^n C_1 x + {}^n C_2 x^2 + \dots + {}^n C_n x^n$

... (i)

Put x = 3 in (i), we get

${}^n C_0 + 3 {}^n C_1 + 3^2 {}^n C_2 + \dots + 3^n {}^n C_n = 4^n$

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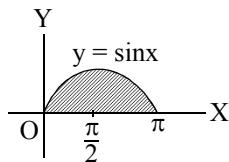
37. (c) $k \cdot 2^{k-1} = 80$
 $\Rightarrow k = 5$

38. (d) $y = e^{-x}$
 $\frac{dy}{dx} = -e^{-x}$
 $\frac{d^2y}{dx^2} = e^{-x}$
 $\frac{d^3y}{dx^3} = -e^{-x} = -y$

39. (c) $\int \frac{dx}{1-x^2} = \frac{1}{2} \ln \left| \frac{1+x}{1-x} \right| + c$

40. (d) Slope of normal $= -\frac{dx}{dy}$
 $\Rightarrow \tan \frac{3\pi}{4} = -\left(\frac{dx}{dy} \right)_{(3,4)}$
 $\Rightarrow \left(\frac{dy}{dx} \right)_{(3,4)} = 1 \quad \therefore f'(3) = 1$

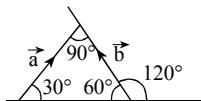
41. (b) Area $= 2 \int_0^{\pi/2} \sin x \, dx$
 $= 2 [-\cos x]_0^{\pi/2} = 2 \text{ sq. units}$



42. (b) $\cosh x = \frac{e^x + e^{-x}}{2}$
 $\sinh x = \frac{e^x - e^{-x}}{2}$
 Then, $\cosh x + \sinh x = \frac{e^x + e^{-x}}{2} + \frac{e^x - e^{-x}}{2} = e^x$

43. (b) Projection of \vec{a} on $\vec{b} = \frac{\vec{a} \cdot \vec{b}}{|\vec{b}|}$
 $= \frac{(2)(1) + (3)(2) + (-2)(3)}{\sqrt{1^2 + 2^2 + 3^2}}$
 $= \frac{2}{\sqrt{14}}$

44. (c) $|\vec{a} + \vec{b}|^2 = |\vec{a}|^2 + |\vec{b}|^2 + 2\vec{a} \cdot \vec{b}$
 $= 1 + 1 + 0 = 2$
 $\therefore |\vec{a} + \vec{b}| = \sqrt{2}$



45. (a) Ratio $= \frac{x_1}{x_2} = \frac{2}{3} = 2 : 3$

46. (d) $(y+1)^2 = -(x-1)$
 $\therefore \text{Vertex} = (1, -1)$ which lies in fourth quadrant.

47. (a) $m_1 + m_2 = m_1 m_2$
 or, $\frac{2h}{7} = \frac{4}{-7} \quad \Rightarrow h = -2$

48. (d) $a^2 = 25 \Rightarrow a = 5$
 $b^2 = 144 \Rightarrow b = 12$
 Length of latus rectum $= \frac{2b^2}{a} = \frac{2 \times 144}{5} = \frac{288}{5}$

49.a 50.b 51.b 52.c 53.b 54.a
 55.d 56.a 57.c 58.a 59.b 60.c

Section – II

61. (b)

 $S_p - S_c = d$
 or, $vt - \frac{1}{2}at^2 = d$
 or, $at^2 - 2vt + 2d = 0$
 $\therefore t = \frac{2v \pm \sqrt{4v^2 - 4a \times 2d}}{2a}$
 Time must be real so $4v^2 - 8ad \geq 0$

62. (b) $\frac{mv^2}{r} = \mu mg$
 or, $v = \sqrt{\mu rg} = \sqrt{0.6 \times 150 \times 10}$
 $= 30 \text{ m/s}$

63. (d) $\Delta PE = \left\{ -\frac{GMm}{r} - \left(-\frac{GMm}{R} \right) \right\}$
 $= GMm \left[\frac{1}{R} - \frac{1}{R+nR} \right]$
 $= gR^2 \cdot m \left(\frac{n+1-1}{R(n+1)} \right)$
 $= mgR \left(\frac{n}{n+1} \right)$

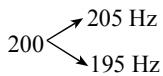
64. (a) Heat lost by steam = Heat gained by water
 or, $m \times 540 + m(100 - 90) = 22(90 - 20)$
 or, $m = \frac{22 \times 70}{560} = 2.75g$

65. (c) $P_T = P_i^o + P_i^N$
 $= (n_0 + n_N) \frac{RT}{V}$

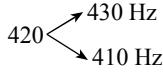
$$= \left(\frac{P_1 V_1}{RT} + \frac{P_2 V_2}{RT} \right) \frac{RT}{V}$$

$$= \frac{1 \times 1 + 2 \times 0.5}{1} = 2 \text{ atm}$$

66. (b)



Again 10 beats/s with 420 Hz produced so



Here second harmonics of 205 Hz can be 410 Hz so frequency is 205 Hz.

67. (d) When capacitors are placed in parallel then

$$C_p = 2C$$

$$V = V_0 e^{-\frac{t}{2CR}}$$

$$\text{or, } \frac{6}{2} = 6 e^{-\frac{t}{2CR}}$$

$$\text{or, } \frac{1}{2} = \frac{1}{e^{-\frac{t}{2CR}}}$$

$$\text{or, } e^{\frac{t}{2CR}} = 2$$

$$\text{or, } \frac{t}{2CR} = \ln 2$$

or, $t = \ln 2 \times 2CR \dots\dots (i)$
When placed in series

$$C_s = \frac{C}{2}$$

$$\text{or, } \frac{6}{2} = 6e^{-\frac{t'}{2C_s R}} \quad \text{or, } \frac{1}{2} = \frac{1}{e^{\frac{t'}{2C_s R}}}$$

$$\text{or, } e^{\frac{t'}{2C_s R}} = 2 \quad \text{or, } \frac{t'}{2C_s R} = \ln 2$$

$$\text{or, } t' = \ln 2 \times \frac{CR}{2} \dots\dots (ii)$$

Dividing (ii) by (i)

$$\frac{t'}{10} = 2 \times 2$$

$$\text{or, } t' = 2.5 \text{ s}$$

68. (b) $I_1^2 R_1 t_1 = I_2^2 R_2 t_2 = ms\Delta\theta$

$$\text{or, } \left(\frac{V}{R_1}\right)^2 \times R_1 \times 15 = \left(\frac{V}{R_2}\right)^2 R_2 t_2$$

$$\text{or, } \frac{V^2}{R_1} \times 15 = \frac{V^2}{R_2} \times t_2$$

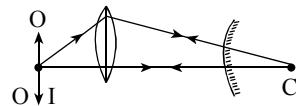
$$\text{or, } \frac{15}{R_1} = \frac{t_2}{\frac{2}{3}R}$$

$$\text{or, } t_2 = 15 \times \frac{2}{3} = 10 \text{ min}$$

69. (b) $I = \frac{d\phi}{dt} = \frac{\frac{NAdB}{R}}{R}$

$$= \frac{10 \times 10 \times 10^{-4} \times 10^8 \times 10^{-4}}{20} = 5 \text{ A}$$

70. (c)



For lens,

$$V = \frac{fu}{u-f} = \frac{20 \times 30}{30-20} = \frac{600}{10} = 60 \text{ cm}$$

$$d = v - r = 60 - 10 = 50 \text{ cm}$$

71. (a) $(\mu - 1)t = n\lambda$

$$\text{or, } \lambda = \frac{(1.5 - 1) \times 6 \times 10^{-6}}{5} = 6 \times 10^{-7} \text{ m} = 6000 \text{ \AA}$$

72. (b) Power = $\frac{nhc}{t\lambda}$

$$\text{or, } \text{Power} = \frac{n}{t} \frac{hc}{\lambda} \times P$$

$$\text{or, } \frac{n}{t} P = \frac{\text{Power}}{C}$$

Force (F) = Rate of change in momentum

$$= 1.6 \frac{n}{t} P$$

$$= 1.6 \times \frac{\text{Power}}{C} = 1.6 \times \frac{60}{3 \times 10^8} = 3.2 \times 10^{-7} \text{ N}$$

73. (b) $E = \phi + eV_s$
 $= 2.75 + 10$
 $= 12.75 \text{ eV}$

Now, $E - E_1 = 12.75$

or, $E = 12.75 - 13.6$

or, $E = -0.85 \text{ eV}$

$$\therefore -\frac{13.6}{n^2} = -0.85 \quad \text{or, } n = 4$$

74. (b) $\frac{C}{C_0} = \left(\frac{1}{2}\right)^{\frac{t}{T_{1/2}}}$

$$\text{or, } \frac{3000}{6000} = \left(\frac{1}{2}\right)^{\frac{140}{T_{1/2}}}$$

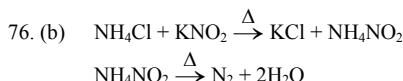
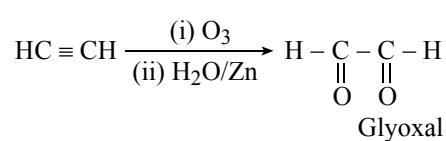
$$\text{or, } T_{1/2} = 140 \text{ days}$$

$$\text{Again, } \frac{C}{C_0} = \left(\frac{1}{2}\right)^{\frac{t}{T_{1/2}}}$$

$$\text{or, } \frac{6000}{C_0} = \left(\frac{1}{2}\right)^{\frac{280}{140}}$$

$$\text{or, } C_0 = 24000 \text{ dps}$$

75. (d)



77. (b)

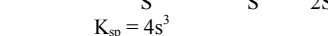
$$78. (d) \frac{W}{E} = \frac{N \times V_{ml}}{1000}, \frac{0.23}{E} = \frac{0.1 \times 30}{1000}$$

$$E = \frac{0.23 \times 1000}{0.1 \times 30} = \frac{230}{3} = 76.67$$

$$\text{MW} = 2 \times 76.67 = 153.3$$

$$\text{Metal oxide} = 153.3 \quad M = 153.3 - 16$$

$$M + 0 = 153.3 \quad M = 137.3$$



$$\text{S} \quad \text{S} \quad 2\text{S}$$

$$K_{sp} = 4\text{S}^3$$

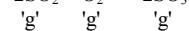
$$S = \sqrt[3]{\frac{1 \times 10^{-11}}{4}} = 1.358 \times 10^{-4} \text{ mol L}^{-1}$$

$$\text{OH}^- = 25 = 2 \times 1.358 \times 10^{-4} = 2.716 \times 10^{-4} \text{ mol/L}^{-1}$$

$$\text{pOH} = \log[2.716 \times 10^{-4}] = 3.566$$

$$\text{pH} = 14 - \text{pOH} = 14 - 3.566 = 10.43$$

80. (c) Number of moles of O_2 used up = $25\% = \frac{25}{100}$
 $= 0.25 \text{ mole}$



$$'g' \quad 'g' \quad 'g'$$

Initial moles: 4 mol 4 mole

At equation (4-2 moles) (4-4 × 0.25 moles) 2 mole

Total no. of moles = 2 + 3 + 2 = 7 moles.

81. (a) $100\text{g of CaCO}_3 = 6.023 \times 10^{23} \text{ no. of C-atoms}$

$$25\text{g of CaCO}_3 = \frac{6.023 \times 10^{23}}{100} \times 25 = 1.5 \times 10^{23}$$

82. (d) For ${}^{7-x}\text{P}_{x-3}$ to be defined, $7 - x > 0 \Rightarrow x < 7$

And, $x - 3 \geq 0 \Rightarrow x \geq 3; 7 - x \geq x - 3$

$$\Rightarrow x \leq 5$$

$$\therefore x \in \{3, 4, 5\} \Rightarrow f(3) = 1, f(4) = 3, f(5) = 2$$

Range = {1, 2, 3}

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83. (d) $\cos\theta = \sin 105^\circ + \cos(90 + 15)$
or, $\cos\theta = \sin 105 - \sin 15$
 $= 2\cos\left(\frac{105+15}{2}\right)\sin\left(\frac{105-15}{2}\right)$
 $= 2\cos 60.\sin 45 = \frac{1}{\sqrt{2}} = \cos\frac{\pi}{4}$
 $\therefore \theta = 2n\pi \pm \frac{\pi}{4}$

84. (c) $\vec{d}_1 = \vec{i} + 2\vec{j} + 3\vec{k}, \vec{d}_2 = -3\vec{i} - 2\vec{j} + \vec{k}$
 $\vec{d}_1 \times \vec{d}_2 = \begin{vmatrix} \vec{i} & \vec{j} & \vec{k} \\ 1 & 2 & 3 \\ -3 & -2 & 1 \end{vmatrix} = 8\vec{i} - 10\vec{j} + 4\vec{k}$
Area $= \frac{1}{2} |\vec{d}_1 \times \vec{d}_2| = \frac{1}{2} \sqrt{8^2 + (-10)^2 + 4^2} = 3\sqrt{5}$

85. (b) $|A| = \begin{vmatrix} 1 & 2 & 1 \\ 2 & 1 & 0 \\ -1 & 0 & 1 \end{vmatrix} = -2$
 $A^{-1} = \frac{1}{|A|} \cdot \text{Adj. } A$

(2, 3) element of $A^{-1} = \frac{1}{|A|} \times \text{cofactor of (3, 2) element of } A$
 $= -\frac{1}{2} \left(- \begin{vmatrix} 1 & 1 \\ 2 & 0 \end{vmatrix} \right) = -\frac{1}{2} \times 2 = -1$

86. (b) $\left[\left(\frac{1-i}{\sqrt{2}} \right)^2 \right]^4 + \left[\left(\frac{1+i}{\sqrt{2}} \right)^2 \right]^4$
 $= \left(\frac{1-2i-1}{2} \right)^4 + \left(\frac{1+2i-1}{2} \right)^4 = (-i)^4 + i^4$
 $= 1 + 1 = 2$

87. (c) $\frac{1}{4} \left(\frac{4}{3 \times 7} + \frac{4}{7 \times 11} + \frac{4}{11 \times 15} + \dots \right)$
 $= \frac{1}{4} \left(\frac{1}{3} - \frac{1}{7} + \frac{1}{7} - \frac{1}{11} + \frac{1}{11} - \frac{1}{15} + \dots \right)$
 $= \frac{1}{4} \times \frac{1}{3} = \frac{1}{12}$

88. (d) $x^2 - 7|x| + 12 = 0$
or, $|x|^2 - 4|x| - 3|x| + 12 = 0$
or, $|x|(|x| - 4) - 3(|x| - 4) = 0$
or, $(|x| - 4)(|x| - 3) = 0$
i.e. $|x| = 4 \Rightarrow x = -4, 4$
& $|x| = 3 \Rightarrow x = -3, 3$
 $\therefore x = -4, -3, 3, 4$

No. of real solutions = 4

89. (a) $a = 1, b = -2, c = 2$

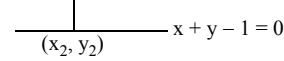
D.C's $l = \frac{1}{\sqrt{6}}, m = -\frac{1}{\sqrt{6}}, n = \frac{2}{\sqrt{6}}$

Required projection $= (x_2 - x_1)l + (y_2 - y_1)m + (z_2 - z_1)n$

$$= 2 \times \frac{1}{\sqrt{6}} + (-6) \left(-\frac{1}{\sqrt{6}} \right) + 2 \times \frac{1}{\sqrt{6}} = 2\sqrt{6}$$

90. (a) Distance between centres = 5
When two circles intersect each other then difference between their radii $<$ distance between centre
 $\Rightarrow r - 3 < 5 \Rightarrow r < 8 \dots \text{(i)}$
Sum of their radii $>$ distance between centres.
 $\Rightarrow r + 3 > 5 \Rightarrow r > 2 \dots \text{(ii)}$
From (i) and (ii), $2 < r < 8$

91. (a) Let the coordinates of foot of perpendicular be (x_2, y_2)
 $(x_1, y_1) = (2, 4)$



$$(x_2, y_2)$$

 $x + y - 1 = 0$

Then, $\frac{x_2 - x_1}{a} = \frac{y_2 - y_1}{b} = \frac{-ax_1 + by_1 + c}{a^2 + b^2}$
i.e. $\frac{x_2 - 2}{1} = \frac{y_2 - 4}{1} = -\frac{(2 + 4 - 1)}{1 + 1}$

From 1st & 3rd, $x_2 = -\frac{1}{2}$

From 2nd & 3rd, $y_2 = \frac{3}{2}$

Required point $= \left(-\frac{1}{2}, \frac{3}{2} \right)$

92. (b) Let $P = \lim_{x \rightarrow 0} x^x$

Then, $\ln P = \lim_{x \rightarrow 0} x \ln x$
 $= \lim_{x \rightarrow 0} \frac{\ln x}{\frac{1}{x}}$
 $= \lim_{x \rightarrow 0} \frac{\frac{1}{x}}{-\frac{1}{x^2}} \text{ [By L' Hospital rule]}$
 $= 0 \quad \therefore P = e^0 = 1$

93. (a) $y = x^2 + \frac{1}{y}$
 $\Rightarrow y^2 = x^2y + 1$

Diff. both sides w.r. to x

$$2y \frac{dy}{dx} = x^2 \frac{dy}{dx} + y \cdot 2x \quad \Rightarrow \frac{dy}{dx} = \frac{2xy}{2y - x^2}$$

94. (b) Let $f(x) = \left(\frac{1}{x} \right)^x = x^{-x} = e^{-x \ln x}$

$f(x) = e^{-x \ln x} (-1 - \ln x)$

For max. or min, $f'(x) = 0 \Rightarrow x = \frac{1}{e}$

$f''(x) = e^{-x \ln x} \left(-\frac{1}{x} \right) + (-1 - \ln x)^2 e^{-x \ln x}$

$\therefore f''\left(\frac{1}{e}\right) = -e \cdot e^{1/e} < 0 \text{ (Max. value)}$

Maximum value $= e^{1/e}$

95. (c) $\int (\sin^{-1}x + \cos^{-1}x) dx$

$$= \int \frac{\pi}{2} dx = \frac{\pi}{2} x + c$$

96. (c) Area $= 2 \int_0^1 y dx = 2 \int_0^1 (1 - |x|) dx$

$$= 2 \int_0^1 (1 - x) dx = 2 \left[x - \frac{x^2}{2} \right]_0^1$$

$$= 2 \left(1 - \frac{1}{2} \right) - 0 = 1$$

97.c

98.c

99.a

100.a

...The End...